

Words vs. graphs: Tracking student understanding of forces

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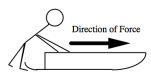

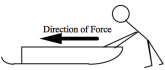
July 18, 2016



The Force and Motion Conceptual Evaluation

- 47-item multiple-choice survey¹
- Several question clusters that assess different topics²

A sled on ice moves in the ways described in questions 1-7 below. *Friction is so small that it can be ignored.* A person wearing spiked shoes standing on the ice can apply a force to the sled and push it along the ice. Choose the one force (A through G) which would **keep the sled moving** as described in each statement below.

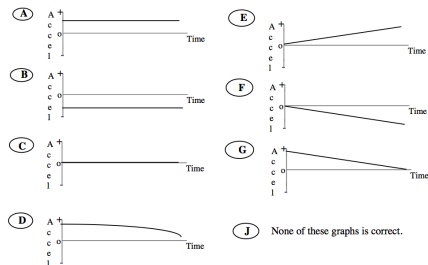
	<p>A. The force is toward the right and is increasing in strength (magnitude).</p> <p>B. The force is toward the right and is of constant strength (magnitude).</p> <p>C. The force is toward the right and is decreasing in strength (magnitude).</p>
	<p>D. No applied force is needed</p>
	<p>E. The force is toward the left and is decreasing in strength (magnitude).</p> <p>F. The force is toward the left and is of constant strength (magnitude).</p> <p>G. The force is toward the left and is increasing in strength (magnitude).</p>

Questions 22-26 refer to a toy car which can move to the right or left on a horizontal surface along a straight line (the + distance axis). The positive direction is to the right.



Different motions of the car are described below. Choose the letter (A to G) of the **acceleration-time** graph which corresponds to the motion of the car described in each statement.

You may use a choice more than once or not at all. If you think that none is correct, answer choice J.

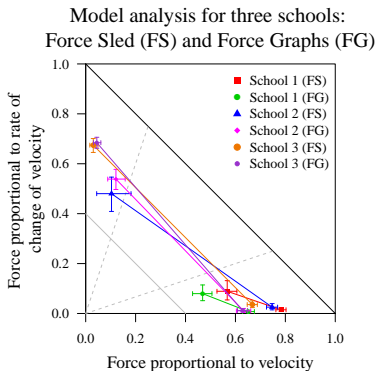
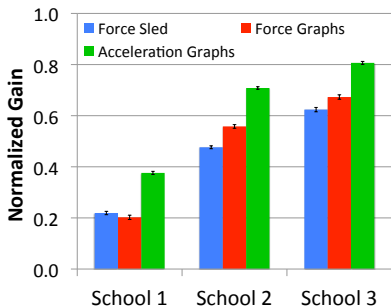


¹R. K. Thornton and D. R. Sokoloff, *Am. J. Phys.* **66**, 338 (1998).

²T. I. Smith and M. C. Wittmann, *Phys. Rev. ST Phys. Educ. Res.* **4**, 020101 (2008).

FMCE: Previous Results

- Normalized gains
- Model analysis³
- Results differ from cluster to cluster as well as from school to school⁴



³L. Bao and E. F. Redish, Phys. Rev. ST Phys. Educ. Res. **2**, 010103 (2006).

⁴T. I. Smith et al., Phys. Rev. ST Phys. Educ. Res. **10**, 020102 (2014).

Isomorphic Questions

Question 1 (Force Sled)

Which force would keep the sled moving toward the right and speeding up at a steady rate (constant acceleration)?

Question 16 (Force Graphs)

The car moves toward the right and is speeding up at a steady rate (constant acceleration).

Question 22 (Acceleration Graphs)

The car moves toward the right (away from the origin), speeding up at a steady rate.

Isomorphic Questions

Question 1 (Force Sled)

Which force would keep the sled moving toward the right and speeding up at a steady rate (constant acceleration)?

Question 16 (Force Graphs)

The car moves toward the right and is speeding up at a steady rate (constant acceleration).

Question 22 (Acceleration Graphs)

The car moves toward the right (away from the origin), speeding up at a steady rate.

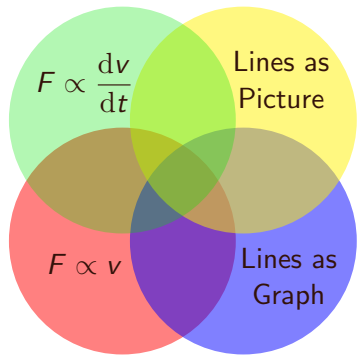
Case 1: Moving to the right and speeding up at a steady rate.

Identifying isomorphic questions

Case	Described Motion	Question		
		FS	FG	AG
1	moving right, speeding up	1	16	22
2	moving right, steady speed	2	14	26
3	moving right, slowing down	3	18	23
4	moving left, speeding up	4	19	25

Underlying Assumptions

- Students use many different mental models⁵ to answer questions on the FMCE
- Different questions and clusters are more or less conducive to particular models
- Many students exist in a superposition state
- Answers depend on both the student and the question



⁵T. I. Smith and M. C. Wittmann, Phys. Rev. ST Phys. Educ. Res. **4**, 020101 (2008), R. J. Beichner, Am. J. Phys. **62**, 750 (1994), L. C. McDermott et al., Am. J. Phys. **55**, 503 (1987)

Contingency Tables

- Compare Force Graphs to Force Sled or Force Graphs to Acceleration Graphs
- Number of students who gave each response pair
- Diagonal cells show within-student coherent responses
- Large numbers show between-students consistent responses
- Cohen's w^6 indicates the strength of the correlation between individual students' responses.⁷
weak: $w < 0.1$; moderate: $w \approx 0.3$; strong: $w > 0.5$
- Ignore models with fewer than 5% of responses on pre- and post-test

		Question 16	
		Correct	Common
Ques. 1	Correct		
	Common		

⁶J. Cohen, *Statistical power analysis for the behavioral sciences*, 2nd (Lawrence Erlbaum Associates, 1988).

⁷R. Rosenblatt and A. F. Heckler, *Phys. Rev. ST Phys. Educ. Res.* **7**, 020112 (2011).

Case 1: Moving right, Speeding up, School 1

Force Sled

Pretest

Force Graphs

$$F \propto \frac{\Delta v}{\Delta t} \quad F \propto v$$

$F \propto \frac{\Delta v}{\Delta t}$	4	9
$F \propto v$	1	181

$w = 0.48$

Force Sled

Post-test

Force Graphs

$$F \propto \frac{\Delta v}{\Delta t} \quad F \propto v$$

$F \propto \frac{\Delta v}{\Delta t}$	39	15
$F \propto v$	17	124

$w = 0.60$

Case 1: Moving right, Speeding up, School 1

Pretest

Force Sled

Force Graphs

$F \propto \frac{\Delta v}{\Delta t}$ $F \propto v$

$F \propto \frac{\Delta v}{\Delta t}$	4	9
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Force Graphs

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- Within-student coherence increases

Case 1: Moving right, Speeding up, School 1

Pretest

Force Sled

Force Graphs

$$F \propto \frac{\Delta v}{\Delta t} \quad F \propto v$$

$F \propto \frac{\Delta v}{\Delta t}$	4	9
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Post-test

Force Sled

Force Graphs

$$F \propto \frac{\Delta v}{\Delta t} \quad F \propto v$$

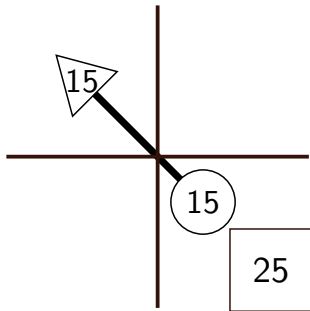
$F \propto \frac{\Delta v}{\Delta t}$	39	15
$F \propto v$	17	124

$w = 0.60$

- Within-student coherence increases
- How do individual students change from pre to post?

Consistency Plots

- Visualizing student transitions between table cells⁸
- “Arrows” show the number of students who went from one pair of pretest responses to a different pair
 - Start in circles (pretest)
 - End in triangles (post-test)
- Squares show students who did not change their answers



⁸M. C. Wittmann and K. E. Black, Phys. Rev. ST Phys. Educ. Res. **10**, 010114 (2014)

Case 1: Moving right, Speeding up

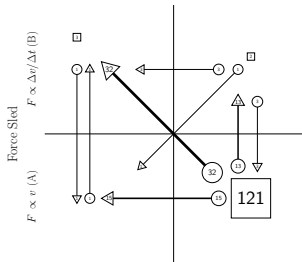
School 1

$N = 195$

Force Graphs

$F \propto \Delta v / \Delta t$ (A)

$F \propto v$ (C)



Pretest

Post-test

4	9	39	15
1	181	17	124

$w = 0.48$

$w = 0.60$

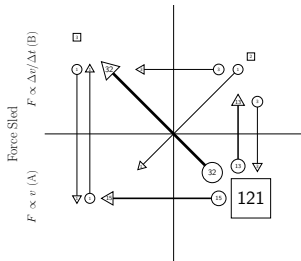
Case 1: Moving right, Speeding up

School 1

$N = 195$

Force Graphs

$F \propto \Delta v / \Delta t$ (A) $F \propto v$ (C)



Pretest

Post-test

4	9	39	15
1	181	17	124

$w = 0.48$

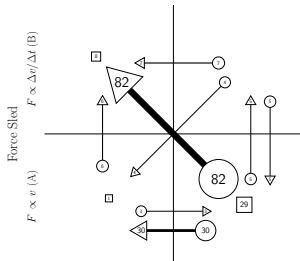
$w = 0.60$

School 2

$N = 180$

Force Graphs

$F \propto \Delta v / \Delta t$ (A) $F \propto v$ (C)



Pretest

Post-test

8	16	103	5
10	146	35	37

$w = 0.31$

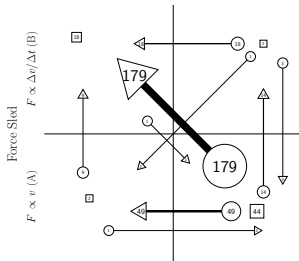
$w = 0.54$

School 3

$N = 340$

Force Graphs

$F \propto \Delta v / \Delta t$ (A) $F \propto v$ (C)



Pretest

Post-test

19	23	224	15
12	286	52	49

$w = 0.47$

$w = 0.49$

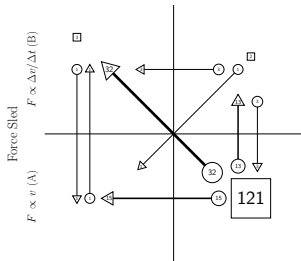
Case 1: Moving right, Speeding up

School 1

$N = 195$

Force Graphs

$F \propto \Delta v / \Delta t$ (A) $F \propto v$ (C)



Pretest

Post-test

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1	181	17	124

$w = 0.48$

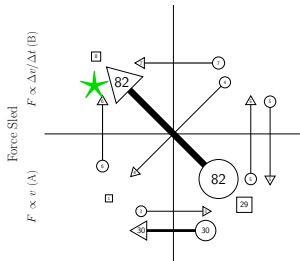
$w = 0.60$

School 2

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Force Graphs

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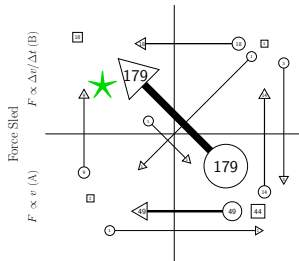
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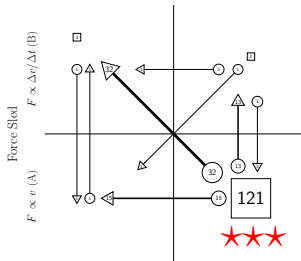
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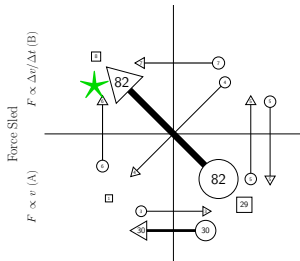
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Force Graphs

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Post-test

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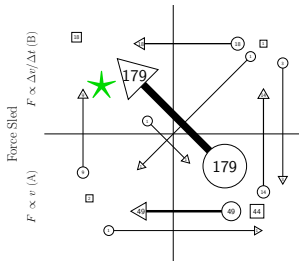
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Force Graphs

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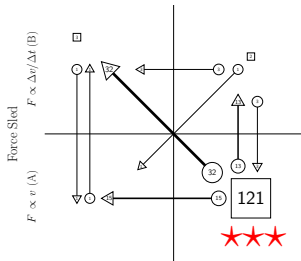
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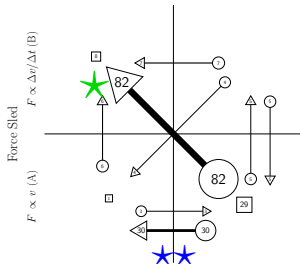
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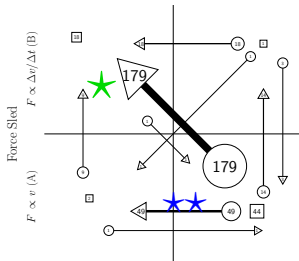
$w = 0.54$

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Pretest

Post-test

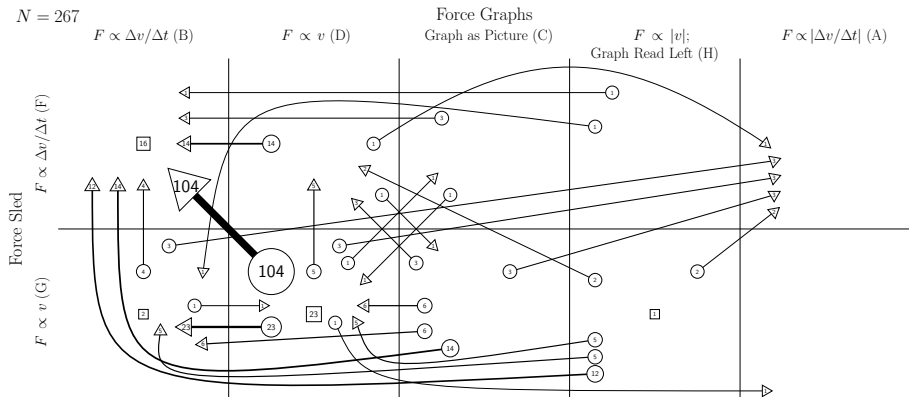
19	23	224	15
12	286	52	49

$w = 0.47$

$w = 0.49$

Case 4: Moving left, Speeding up, School 3

$N = 267$



Pretest

16	16	4	2	0
10	160	32	27	0

$w = 0.45$

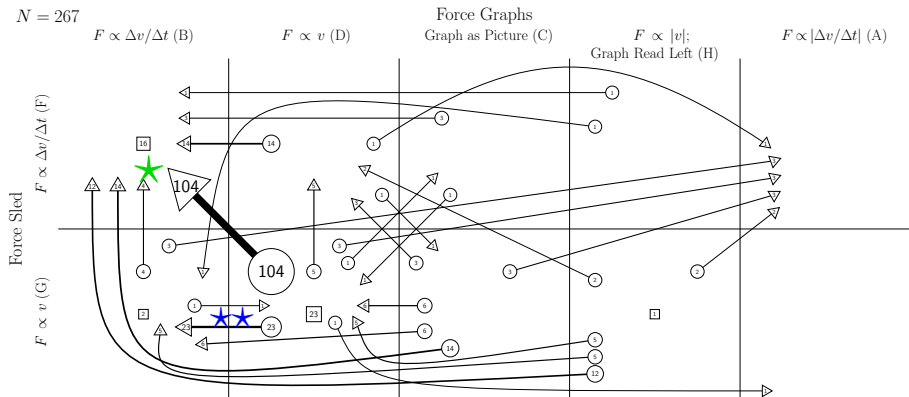
Post-test

168	10	1	0	12
37	36	1	1	1

$w = 0.52$

Case 4: Moving left, Speeding up, School 3

$N = 267$



Pretest

16	16	4	2	0
10	160	32	27	0

$w = 0.45$

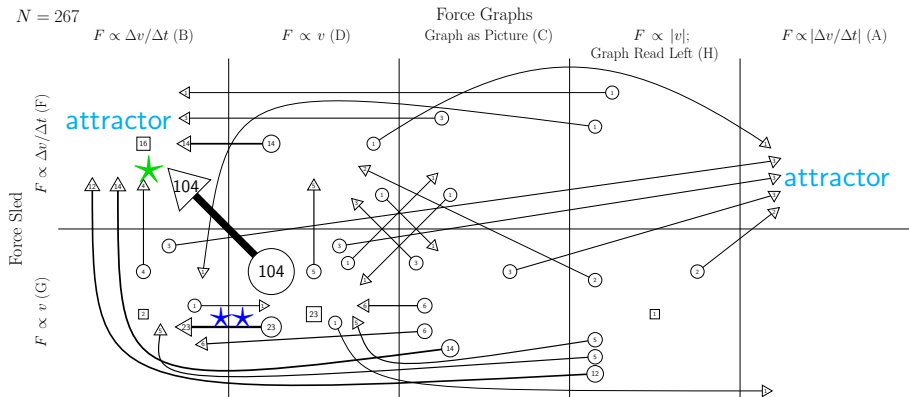
Post-test

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37	36	1	1	1

$w = 0.52$

Case 4: Moving left, Speeding up, School 3

$N = 267$



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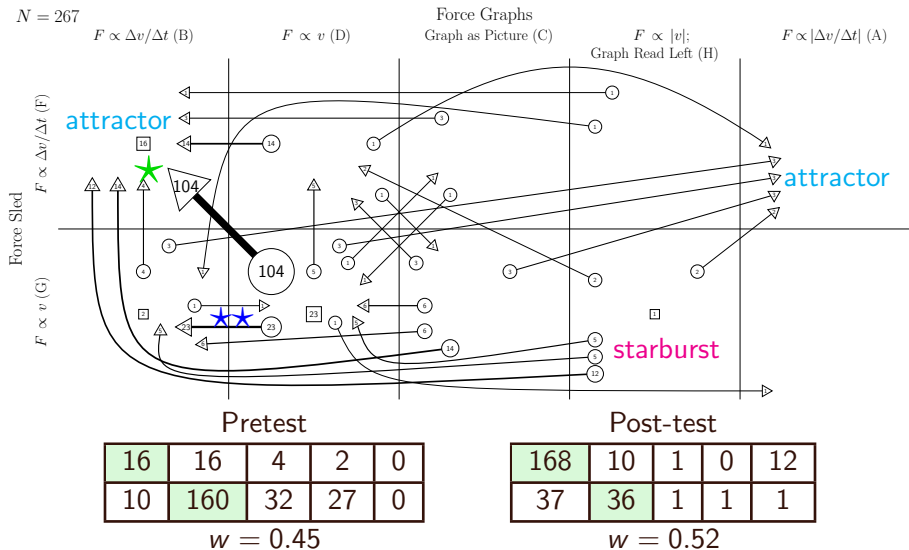
Post-test

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37	36	1	1	1

$w = 0.52$

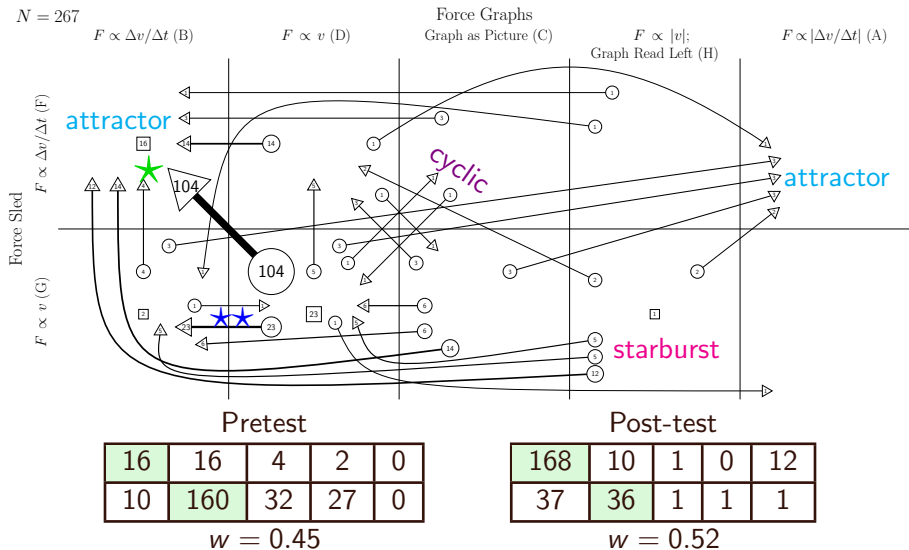
Case 4: Moving left, Speeding up, School 3

$N = 267$



Case 4: Moving left, Speeding up, School 3

$N = 267$



Comparing Schools: Statistical Analyses

ANOVA results for individual student normalized gains with Tukey HSD *post hoc* comparisons between schools ($p < 0.05$); * indicates $p < 0.001$.

	Average g			Main Eff.	p -values		
	S1	S2	S3		1v2	1v3	2v3
Full FMCE	0.29	0.60	0.69	*	*	*	0.003
Cases 1–4	0.23	0.61	0.71	*	*	*	0.02
Case 1	0.31	0.65	0.77	*	*	*	0.007

S3>S2>S1

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Cases 1-4	0.23	0.61	0.71	*	*	*	0.02
Case 1	0.31	0.65	0.77	*	*	*	0.007

$S3 > S2 > S1$

Comparison of consistency plots using χ^2 test of independence ($p < 0.05$) with the Bonferroni correction for *post hoc* comparisons (pairwise: $p < 0.013$).

	Main Eff.	1v2	1v3	2v3
Case 1	*	*	*	0.24
Case 2	*	*	*	0.65
Case 3	*	*	*	0.49
Case 4	*	*	*	0.07

$S3 = S2 > S1$

Summary of Results

- Explicitly treating students as being in a superposition state of mental models
- Different approaches reveal discrepant similarities and differences
 - Normalized gains and model analysis: $S3 > S2 > S1$
 - Consistency plots: $S3 = S2 > S1$
- Most students at Schools 2 and 3 go from common incorrect to correct on all questions
- More students increase on Force Graphs than Force Sled, and more on Acceleration Graphs than Force Graphs
- Most students at School 1 stay in the common incorrect cell on all questions
- Contingency tables with Cohen's w show within-student coherence increasing over time
- Many different transitions for Case 4: “beginning state” + “instruction” \neq “ending state”
- Possible hierarchy of incorrect responses:⁹ starbursts may represent very naïve responses (only pretest); attractors may represent more sophisticated ones (only post-test)
- Cyclic transitions only visible on consistency plots

⁹R. K. Thornton, AIP Conf. Proc. 399, 241 (1997)

- Synthesize results across cases
- Conduct interviews to test model definitions
- Developing statistic to report between-students consistency
- Closely examine similarities and differences between the instruction at each school



Rowan University Physics Education Research Team: Summer 2016



Partially supported by a PhysTEC comprehensive site award

Upcoming Posters

More Results!

Poster PST1-D12, 9:15-10:00 tonight!

More Detailed Methodology

PERC Poster Symposium: Expanding Research Questions by Expanding
Quantitative Methodologies

Parallel Session I, Thurs. 7/21/16, 10:30 am (Bataglieri Room)

email: smithtr@rowan.edu